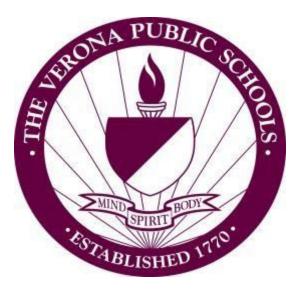
# Verona Public School District Curriculum Overview

# **Trigonometry**



Curriculum Committee Members: Danielle Mutovic Jonathan Thai

Supervisor: Glen Stevenson

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Verona Public Schools 121 Fairview Ave., Verona, NJ 07044 www.veronaschools.org

#### Verona Public Schools Mission Statement:

The mission of the Verona Public Schools, the center of an engaged and supportive community, is to empower students to achieve their potential as active learners and productive citizens through rigorous curricula and meaningful, enriching experiences.

#### **Course Description:**

This course is designed for students who have completed Algebra II, but are not planning on majoring in a STEM-related field. This course will cover topics in a standard college-level Trigonometry course, Elementary Trigonometry, Analytic Trigonometry, Vectors, Complex Numbers and Conic Sections. These topics will be put in the context of real world applications. Graphing calculators will be an important tool that will routinely be used in instruction.

Prerequisite(s): Algebra 2 CP



Standard 8: Technology Standards	
8.1: Educational Technology: All students will use digital tools to access, manage,	8.2: Technology Education, Engineering, Design, and Computational Thinking -
evaluate, and synthesize information in order to solve problems individually and	Programming: All students will develop an understanding of the nature and impact of technology,
collaborate and to create and communicate knowledge.	engineering, technological design, computational thinking and the designed world as they relate to the
	individual, global society, and the environment.
X A. Technology Operations and Concepts	X A. The Nature of Technology: Creativity and Innovation
X B. Creativity and Innovation	B. Technology and Society
C. Communication and Collaboration	C. Design
D. Digital Citizenship	D. Abilities for a Technological World
E. Research and Information Fluency	E. Computational Thinking: Programming
X F. Critical thinking, problem solving, and decision making	

SEL Competencies and Career Ready Practices		
Social and Emotional Learning Core Competencies: These competencies are	<b>Career Ready Practices:</b> These practices outline the skills that all individuals need to have	
identified as five interrelated sets of cognitive, affective, and behavioral	to truly be adaptable, reflective, and proactive in life and careers. These are researched	
capabilities	practices that are essential to career readiness.	
Self-awareness: The ability to accurately recognize one's emotions and thoughts and	X CRP2. Apply appropriate academic and technical skills.	
their influence on behavior. This includes accurately assessing one's strengths and	CRP9. Model integrity, ethical leadership, and effective management.	
limitations and possessing a well-grounded sense of confidence and optimism.	X CRP10. Plan education and career paths aligned to personal goals.	
Self-management: The ability to regulate one's emotions, thoughts, and behaviors	CRP3. Attend to personal health and financial well-being.	
effectively in different situations. This includes managing stress, controlling	X CRP6. Demonstrate creativity and innovation.	
impulses, motivating oneself, and setting and working toward achieving personal	X CRP8. Utilize critical thinking to make sense of problems and persevere in solving them.	
and academic goals.	CRP11. Use technology to enhance productivity.	
Social awareness: The ability to take the perspective of and empathize with others from	X CRP1. Act as a responsible and contributing citizen and employee.	
diverse backgrounds and cultures, to understand social and ethical norms for	CRP9. Model integrity, ethical leadership, and effective management.	
behavior, and to recognize family, school, and community resources and supports.		
Relationship skills: The ability to establish and maintain healthy and rewarding	X CRP4. Communicate clearly and effectively and with reason.	
relationships with diverse individuals and groups. This includes communicating	CRP9. Model integrity, ethical leadership, and effective management.	
clearly, listening actively, cooperating, resisting inappropriate social pressure,	CRP12. Work productively in teams while using cultural global competence.	
negotiating conflict constructively, and seeking and offering help when needed.		
Responsible decision making: The ability to make constructive and respectful choices	X CRP5. Consider the environmental, social, and economic impact of decisions.	
about personal behavior and social interactions based on consideration of ethical	CRP7. Employ valid and reliable research strategies.	
standards, safety concerns, social norms, the realistic evaluation of consequences	X CRP8. Utilize critical thinking to make sense of problems and persevere in solving them.	
of various actions, and the well-being of self and others.	CRP9. Model integrity, ethical leadership, and effective management.	

Standard 9: 21 <sup>st</sup> Century Life and Careers		
<b>9.1: Personal Financial Literacy:</b> This standard outlines the important fiscal knowledge, habits, and skills that must be mastered in order for students to make informed decisions about personal finance. Financial literacy is an integral component of a student's college and career readiness, enabling students to achieve fulfilling, financially-secure, and successful careers.	<b>9.2: Career Awareness, Exploration &amp; Preparation:</b> This standard outlines the importance of being knowledgeable about one's interests and talents, and being well informed about postsecondary and career options, career planning, and career requirements.	<b>9.3: Career and Technical Education:</b> This standard outlines what students should know and be able to do upon completion of a CTE Program of Study.
<ul> <li>X A. Income and Careers</li> <li>B. Money Management</li> <li>C. Credit and Debt Management</li> <li>X D. Planning, Saving, and Investing</li> <li>X E. Becoming a Critical Consumer</li> <li>F. Civic Financial Responsibility</li> <li>G. Insuring and Protecting</li> </ul>	<ul> <li>A. Career Awareness (K-4)</li> <li>B. Career Exploration (5-8)</li> <li>X C. Career Preparation (9-12)</li> </ul>	<ul> <li>A. Agriculture, Food &amp; Natural Res.</li> <li>B. Architecture &amp; Construction</li> <li>C. Arts, A/V Technology &amp; Comm.</li> <li>D. Business Management &amp; Admin.</li> <li>E. Education &amp; Training</li> <li>F. Finance</li> <li>G. Government &amp; Public Admin.</li> <li>H. Health Science</li> <li>I. Hospital &amp; Tourism</li> <li>J. Human Services</li> <li>K. Information Technology</li> <li>L. Law, Public, Safety, Corrections &amp; Security</li> <li>M. Manufacturing</li> <li>N. Marketing</li> <li>X O. Science, Technology, Engineering &amp; Math</li> <li>P. Transportation, Distribution &amp; Log.</li> </ul>

Course Materials	
<b>Core Instructional Materials</b> : These are the board adopted and approved materials to support the curriculum, instruction, and assessment of this course.	<b>Differentiated Resources</b> : These are teacher and department found materials, and also approved support materials that facilitate differentiation of curriculum, instruction, and assessment of this course.
<ul> <li>TI-Nspire CX Calculator</li> <li>Trigonometry with Calc Chat and Calc View (10 E)</li> </ul>	<ul> <li>Khan Academy</li> <li>Delta Math</li> <li>Kuta Software</li> <li>TI-Nspire CX CAS Student Software</li> <li>SmartBoard and SMART Notebook 10 Software</li> <li>Google Classroom, Sheets, Slides, and Documents</li> </ul>



Unit Title / Topic: Elementary Trigonometry	Unit Duration: 17 Class periods	
Stage 1: Desired Results		
Established Goals: F.TF.1 - Understand radian measure of an angle as the length of the arc on the unit circle subtended by the angle.		
F.TF.2 - Explain how the unit circle in the coordinate plane enables the extension of trigon	ometric functions to all real numbers, interpreted as radian measures of angles traversed	
counterclockwise around the unit circle.		
F.TF.3 - Use special triangles to determine geometrically the values of sine, cosine, tanger	It for $\pi/3$ , $\pi/4$ and $\pi/6$ , and use the unit circle to express the values of sine, cosine, and	
tangent for $\pi -x$ , $\pi +x$ , and $2\pi -x$ in terms of their values for x, where x is any real number.		
F.TF.4 - Use the unit circle to explain symmetry (odd and even) and periodicity of trigonor	netric functions.	
F.TF.5 - Choose trigonometric functions to model periodic phenomena with specified amp	litude, frequency, and midline.	
F.TF.6 - Understand that restricting a trigonometric function to a domain on which it is alw G.SRT.6 - Understand that by similarity, side ratios in right triangles are properties of the		
<b>G.SRT.7</b> - Explain and use the relationship between the sine and cosine of complementary		
<b>G.SRT.8</b> - Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in	-	
Transfer Goal:		
Students will be able to independently use their learning to		
apply their knowledge of the graphs of periodic functions and their equivalents to recogniz	e and analyze real-life periodic phenomena that have these properties.	
analyze real life phenomena while keeping in mind the unit circle, its implications and its r	elationships.	
Students will understand that:	Essential Questions:	
Trig functions are ratios of sides of right triangles	What are examples of things that happen periodically?	
• Trig functions evaluated at a certain angle are constant, regardless of the size of the triangle	<ul> <li>How can radian measures be used in the real world?</li> <li>What is the value of knowing trigonometric identities?</li> </ul>	
<ul> <li>Trig identities allow us to express trig expressions in different, but equivalent ways</li> <li>Radians are often a more appropriate way of describing angles</li> </ul>	<ul> <li>What is the value of knowing trigonometric identities?</li> <li>What is the benefit of having different units of measure?</li> </ul>	
<ul> <li>Changes to the algebraic equation of a function cause predictable changes to the function's</li> </ul>	<ul> <li>What is the benefit of having different representations?</li> </ul>	
graph	• How can the unit circle begin to explain the graphs of sin, cos, tan, cot, sec and csc?	
Basic properties of trig graphs can be linked to a deep understanding of the unit circle and		
fundamental trig identities         Students will know:       Students will be able to:		
Basic trig identities	Solve multiple angle trig problems	
Pythagorean identities	Derive trig formula	
Cofunction relationships	Compose ordinates of sinusoidal graphs	
<ul> <li>Basic trig functions of 30, 45 60 degree angles</li> </ul>	<ul> <li>Analyze and write the equations for sinusoidal graphs</li> </ul>	
• The relationship between (cos, sin) and (x, y) on the unit circle	Solve basic right triangle trig word problems	
<ul> <li>Sin, cos and tan of 30, 45, 60</li> <li>Sin, cos and tan of guadrantal angles</li> </ul>	<ul> <li>Convert between radians and degrees</li> <li>Evaluate a trigonometric function for any multiple of 30, 45, 60 or 90</li> </ul>	
<ul> <li>Period formulas</li> </ul>	<ul> <li>Find all six trig functions of an angle, given one</li> </ul>	
<ul> <li>Relationship between frequency, amplitude, volume and pitch</li> </ul>	<ul> <li>Fill out a unit circle (angles in radians, coordinates of points)</li> </ul>	
5 Graphical Critical Points		
Inverse trig functions		
Stage 2: Acceptable Evidence		

#### Transfer Tasks -

- <u>Graphing Trig Functions Project</u> Students will analyze average monthly temperatures (or another sinusoidal set of data) in a city of their choice. They will apply their knowledge of periodic functions to analyze this periodic phenomenon
- Students will analyze dissonant and consonant sound intervals. Students will analyze intervals that sound pleasing and intervals that sound displeasing, and students will uncover the relationship between frequency and pitch, as well as amplitude and volume.
- Chapter 13 Performance Tasks Graphs and the Unit Circle Students will answer real world/graphical questions relating to the topics in Chapter 13
- <u>Chapter 14 Performance Tasks</u> Trig Identities, Right/Non-Right Triangle Trig Students will answer real world/graphical questions relating to the topics in Chap 14

- Trigonometry with Calc Chat and Calc View (10 E)
- TI-Nspire Lesson Activities: <u>https://education.ti.com/en/timathnspired/us/precalculus</u>
- Summary Graphing Sine and Cosine
- Investigate Changes to Trig Graphs
- Graphing Trig Functions Investigation Problem Set
- Graphing Trig Functions Review
  - Graphing Trig Functions Review Answers
- Graphs of Sound Waves for Last Section of Graphing Trig Functions
- Graphing Trig Functions Teacher Notes
- Graphing Trig Functions Student Notes
- <u>Trig Graph Transformations Worksheet</u>
  - Trig Graph Transformation Worksheet Answers
- Graphing Trig Functions Review CP
- <u>Steps for Graphing Trig Functions CP</u>
- Trig Identities CP
- Khan Academy Trig Graphs
- <u>Regents Exam Questions by topic</u>
- <u>Math Videos By Topic</u>



- <u>Khan Academy Modeling Periodic Functions</u>
- <u>Regents Prep Arc Length and Radian Measure</u>
- Regents Prep Trig Graphing and Translation
- Another Ferris Wheel Scaffolded Example
- <u>More complex Ferris Wheel Scaffolded Example</u>
- <u>Math Assessment Project Tasks by Standard</u>
- <u>Unit Circle</u> Printable Unit circle with degrees, radians, sine and cosine values
- <u>Trigonometric Identities</u> Basic Trig Identities reference sheet



Unit Title / Topic: Analytic Trigonometry	Unit Duration: 11 Class periods	
Stage 1: Desired Results		
Established Goals: F.TF.5 - Choose trigonometric functions to model periodic phenomena with specified amplitude, frequency, and midline. F.TF.6 - Understand that restricting a trigonometric function to a domain on which it is always increasing or always decreasing allows its inverse to be constructed.		
<b>F.TF.7</b> - Use inverse functions to solve trigonometric equations that arise in modeling contexts; eva		
<b>F.TF.8</b> - Prove the Pythagorean identity $\sin^2(\theta) + \cos^2(\theta) = 1$ and use it to find $\sin(\theta)$ , $\cos(\theta)$ , or $\tan(\theta)$		
<b>F.TF.9</b> - Prove the addition and subtraction formulas for sine, cosine and tangent and use them to s		
<b>F.IF.4</b> - For a function that models a relationship between two quantities, interpret key features of g		
descriptions of the relationship.		
F.IF.7 - Graph functions expressed symbolically and show key features of the graph, by hand in sin	nple cases and using technology for more complicated cases. Graph exponential and logarithmic	
functions, showing intercepts and end behavior, and trigonometric functions, showing period, midlin	ne, and amplitude.	
F.IF.8 - Write a functions defined by an expression in different but equivalent forms to reveal and expression in different but equivalent forms to reveal and expression in different but equivalent forms to reveal and expression in the second seco	xplain different properties of the function.	
<b>F.IF.9</b> - Compare properties of two functions each represented in a different way (algebraically, gra	phically, numerically in tables or by verbal descriptions).	
<b>F.BF.1 -</b> Write a function that describes a relationship between two quantities.		
<b>F.BF.3</b> – Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$ , $k f(x)$ , $f(kx)$ , and $f(x + k)$ for spe	cific values of k (both positive and negative); find the value of k given the graphs. Experiment	
with cases and illustrate an explanation of the effects on the graph using technology. Include recog		
<b>A.REI.2</b> - Understand solving equations as a process of reasoning and explain the reasoning.		
<b>Transfer Goal:</b> Students will be able to <u>independently</u> use their learning to logically realize and explain t	the benefits of proofs (Identities) in mathematics.	
Students will understand that:	Essential Questions:	
<ul> <li>Fundamental trig identities are commonly seen in many parts of calculus</li> <li>Trigonometric identities enable us to rewrite trig equations that model real life situations</li> <li>Trig identities allow us to express trig expressions in different, but equivalent ways</li> <li>Trig equations can be treated like much more basic equations by using the concept of substitution</li> <li>Trigonometric functions are the basis of many Physics properties including sounds waves and simple harmonic motion.</li> <li>Trigonometric Equations have infinitely many solutions</li> <li>Trig equations have many applications in circular motion</li> <li>SUm and Dlfference formulas are used to model standing waves</li> </ul>	<ul> <li>What is the value of knowing trigonometric identities?</li> <li>What is the relationship between a trig equation and the trig functions graph?</li> <li>How can we determine if an arc trig function will yield multiple angles in a given interval?</li> <li>What is the algebraic and graphical relationship between trig equations and quadratic/linear equations?</li> <li>What is the relationship between sounds waves, simple harmonic motion and trig functions?</li> <li>Why do trigonometric equations have infinitely many solutions?</li> <li>How can we express infinitely many solutions?</li> <li>What mathematical logic can be used to explain projectile motion?</li> </ul>	
Students will know:	Students will be able to:	
Fundamental Trig Identities	Verify Trigonometric Identities	
<ul> <li>Inverse trig functions</li> <li>Sum and Difference Formulas</li> </ul>		
Sum and Difference Formulas     Double and Half Angle Formulas	<ul> <li>Solve linear trig equations</li> <li>Solve quadratic trig equations</li> </ul>	
Algebraic Techniques to solve trig equations	<ul> <li>Solve trig equations with more than one function</li> </ul>	
<ul> <li>Quadratic techniques to solve trig equations</li> <li>Cofunction Identities</li> </ul>	Solve trig equations graphically     Solve multiple angle trig problems	
Reduction Identities	<ul> <li>Solve multiple angle trig problems</li> <li>Derive trig formula</li> </ul>	
Power-Reducing Formulas	Compose ordinates of sinusoidal graphs	
Product to Sum and Sum to Product formulas	Analyze and write the equations for sinusoidal graphs	
Stage 2: Acceptable Evidence		
Transfer Task		
Analytic Trig Transfer Task - Students will use their knowledge of trigonometric identities and their u	uses to create a playable game made to reinforce concepts	

- Trigonometry with Calc Chat and Calc View (10 E)
- TI-Nspire Lesson Activities: <a href="https://education.ti.com/en/timathnspired/us/precalculus">https://education.ti.com/en/timathnspired/us/precalculus</a>
- <u>Solving Trig Equations Investigation</u>
- Solving Trig Equations Exam Review
  - Solving Trig Equations Exam Review Answers
- <u>Solving Trig Equations Teacher Notes Honors</u>
- Solving Trig Equations Student Notes Honors
- Khan Academy Trig Equations
- <u>Summative Assessment Tasks</u>



Unit Title / Topic: Additional Topics in Trigonometry	Unit Duration: 9 Class periods	
Stage 1: Desired Results		
Established Goals: G.SRT.9 - Derive the formula A = 1/2 ab sin(C) for the area of a triangle by drawing an auxiliary line from a vertex perpendicular to the opposite side.		
G.SRT.10 - Prove the Laws of Sines and Cosines and use them to solve problems.		
<b>G.SRT.11</b> - Understand and apply the Law of Sines and the Law of Cosines to find unknown mea	suraments in right and non-right triangles (e.g., surveying problems, resultant forces)	
<b>N-VM.1</b> . (+) Recognize vector quantities as having both magnitude and direction. Represent vector	or quantities by directed line segments, and use appropriate symbols for vectors and their	
magnitudes (e.g., v,  v ,   v  , v).		
<b>N-VM.2</b> . (+) Find the components of a vector by subtracting the coordinates of an initial point from	the coordinates of a terminal point.	
<b>N-VM.3</b> . (+) Solve problems involving velocity and other quantities that can be represented by vec	tors.	
N-VM.4. (+) Add and subtract vectors.		
N-VM.4.a. Add vectors end-to-end, component-wise, and by the parallelogram rule. Understand th	nat	
the magnitude of a sum of two vectors is typically not the sum of the magnitudes.		
<b>N-VM.4.b</b> . Given two vectors in magnitude and direction form, determine the magnitude and direction	tion of their sum.	
<b>N-VM.4.c.</b> Understand vector subtraction $v - w$ as $v + (-w)$ , where $-w$ is the additive inverse of w,		
subtraction graphically by connecting the tips in the appropriate order, and perform vector subtrac	uon component-wise.	
<b>N-VM.5.</b> (+) Multiply a vector by a scalar.		
<b>N-VM.5.a</b> . Represent scalar multiplication graphically by scaling vectors and possibly reversing the		
<b>N-VM.5.b</b> . Compute the magnitude of a scalar multiple $cv$ using $  cv   =  c v$ . Compute the direction	n of cv knowing that when $ c v \neq 0$ , the direction of cv is either along v (for c > 0) or against v	
(for $c < 0$ ).		
Students will be able to <u>independently</u> use their learning to solve a variety of problems the Physics.		
Students will understand that:	Essential Questions:	
• The LoC, LoS and Area formula are generalized versions of Pythagorean Theorem,	What is the relationship of the Law of Cosines, Law of Sines and area formula to	
<ul> <li>SohCahToa and A=1/2bh</li> <li>Trigonometry allows you to find distances or angles that you could not have measured</li> </ul>	<ul><li>theorems you previously learned?</li><li>What is the utility of the Law of Sines and the Law of Cosines?</li></ul>	
<ul> <li>The law of sines can be used in cases where AAS, ASA and SSA are satisfied</li> </ul>	<ul> <li>What is the duility of the Law of Sines and the Law of Cosines?</li> <li>How can trigonometry be used in the real world?</li> </ul>	
<ul> <li>The ambiguous case must be checked when SSA is satisfied</li> </ul>	<ul> <li>How does changing one part of a triangle affect other parts of the triangle?</li> </ul>	
• The Law of Cosines can be used in cases where SSS and SAS are satisfied	Why does an ambiguous case exist?	
<ul> <li>There is no ambiguous case in LoC</li> </ul>	<ul> <li>Why do both magnitude and direction matter?</li> </ul>	
Vectors are useful tools in solving real-life problems	How are math and physics related?	
Students will know:	Students will be able to:	
Law of Cosines	Use the Law of Sines	
<ul> <li>Law of Sines</li> <li>Area Formula</li> </ul>	<ul> <li>Use the Law of Cosines</li> <li>Use Heron's Area Formula</li> </ul>	
Heron's Area Formula	Solve area problems	
Directed line segment	Solve force problems	
Initial point	Write the component form of a vector	
Terminal point	Calculate the magnitude of a vector	
Magnitude	Perform vector operations	
• Vector	Use Properties of vector Addition	
Unit vector     Standard position	Use Properties of Scalar Multiplication     Solve Device Drablema involving vectors	
<ul> <li>Standard position</li> <li>Parallelogram Law</li> </ul>	<ul> <li>Solve Physics Problems involving vectors</li> <li>Calculate dot products of vectors</li> </ul>	
Resultant	Use properties of dot products	
Negative vector	• Find the angle between 2 vectors	
Direction Angles	Find vector components	

Transfer Task

Orthogonal vectors

## Stage 2: Acceptable Evidence

• Decompose a vector

<u>TrigStar Competition</u> - Students will be introduced to trigonometry in the real world through a local competition facilitated by the National Society of Professional Surveyors.

Cross Curricular Vector Task - Print out road map of Verona. Have students locate their home. Then have them map out their walk/drive to VHS making sure to approximate roads as straight lines, not curves. have them do vector decomposition on each of the vectors, add them up and determine the magnitude and direction of their total displacement from their home. Then the students can measure the straight-line distance of their house from VHS from the map and see how close they got to the actual answer. You can then talk about vectors (displacement) vs scalars (distance) and even bring velocity (vector) and speed (scalar) into the discussion and do a bit of r=dt.

- Kuta Software
- Trigonometry with Calc Chat and Calc View (10 E)
- Law of Sines Students Notes CP
- Law of Cosines Student Notes CP
- <u>Reference Angles CP</u>
- <u>Khan Academy Non-Right Triangle Trig</u>
- Khan Academy Unit Circle
- <u>Khan Academy- Vectors</u>
- Summative Assessment Tasks



#### Unit Title / Topic: Complex Numbers

### Unit Duration: 11 Class Periods

# Stage 1: Desired Results

#### **Established Goals:**

N-CN.1. Know there is a complex number i such that  $i^2 = -1$ , and every complex number has the form a + bi with a and b real.

N-CN.2. Use the relation  $i^2 = -1$  and the commutative, associative, and distributive properties to add, subtract, and multiply complex numbers.

N-CN.3. (+) Find the conjugate of a complex number; use conjugates to find moduli and quotients of complex numbers.

N-CN.4. (+) Represent complex numbers on the complex plane in rectangular and polar form (including real and imaginary numbers), and explain why the rectangular and polar forms of a given complex number represent the same number.

*N-CN.5.* (+) Represent addition, subtraction, multiplication, and conjugation of complex numbers geometrically on the complex plane; use properties of this representation for computation. For example,  $(-1 + \sqrt{3}i)3 = 8$  because  $(-1 + \sqrt{3}i)$  has modulus 2 and argument 120°.

N-CN.6. (+) Calculate the distance between numbers in the complex plane as the modulus of the difference, and the midpoint of a segment as the average of the numbers at its endpoints.

N-CN.C. Use complex numbers in polynomial identities and equations.

N-CN.7. Solve quadratic equations with real coefficients that have complex solutions.

N-CN.8. (+) Extend polynomial identities to the complex numbers. For example, rewrite  $x^2 + 4$  as (x + 2i)(x - 2i).

N-CN.9. (+) Know the Fundamental Theorem of Algebra; show that it is true for quadratic polynomials.

#### Transfer Goal:

Students will be able to independently use their learning to...use complex numbers analytically and graphically.

Students will understand that:	Essential Questions:
Complex numbers are made up of a real part and an imaginary part	• How can we use complex numbers?
Complex solutions occur in conjugate pairs	• How can we use the Fundamental Theorem of Algebra with complex numbers?
Graphing complex numbers is similar to plotting coordinates on the rectangular coordinate plane	<ul> <li>How are the complex plane and rectangular coordinate planes similar and different from one another?</li> </ul>
• Complex numbers can be rewritten in trigonometric form and used in electrical engineering	Why is it important to rewrite complex numbers in trigonometric form?
Students will know:	Students will be able to:
• Complex numbers: $a + bi$	<ul> <li>Use the imaginary unit, i, to write complex numbers</li> </ul>
Complex conjugates	<ul> <li>Add, subtract, and multiply complex numbers</li> </ul>
Principal square root of a negative number	<ul> <li>Use complex conjugates to write the quotient of two complex numbers in standard form</li> </ul>
<ul> <li>Fundamental Theorem of Algebra</li> </ul>	<ul> <li>Find complex solutions of quadratic equations</li> </ul>
Linear Factorization theorem	<ul> <li>Determine the numbers of solutions of polynomial equations</li> </ul>
Complex conjugate theorem	<ul> <li>Find solutions of polynomial equations</li> </ul>
• Zeros	<ul> <li>Find zeros of polynomial functions and find polynomial functions given the zeros of the</li> </ul>
Roots	functions
Complex plane	<ul> <li>Plot complex numbers in the complex plane and find absolute values of complex numbers</li> </ul>
Distance Formula	<ul> <li>Perform operations with complex numbers in the complex plane</li> </ul>
Midpoint Formula	<ul> <li>Use the distance and midpoint formulas in the complex plane</li> </ul>
• Trig form of complex number $a + bi$ is $z = r(cos\theta + i sin\theta)$	<ul> <li>Write trigonometric forms of complex numbers</li> </ul>
	<ul> <li>Multiply and divide complex numbers written in trigonometric form</li> </ul>

### **Stage 2: Acceptable Evidence**

#### **Transfer Task**

Modeling a Quadratic Regression - Students will be asked to complete a quadratic regression with a set of real-world data. They will be asked to compare their quadratic model with the actual data they found through research.

- Trigonometry with Calc Chat and Calc View (10 E)
- <u>Chapter 4 Larson Interactive Activities</u>
- Fundamental Theorem of Algebra Notes
- Khan Academy- Complex Numbers
- Summative Assessment Tasks



Unit Title / Topic: Topics in Analytic Geometry	e / Topic: Topics in Analytic Geometry Unit Duration: 19 Class periods	
Stage 1: Desired Results		
Established Goals: A.CED.3 - Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context. G.GPE.1 - Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation. G.GPE.2 - Derive the equation of a parabola given a focus and directrix. G.GPE.3 - Derive the equations of ellipses and hyperbolas given the foci, using the fact that the sum or difference of distances from the foci is constant Transfer Goal:		
Students will be able to independently use their learning to recognize and identify different conic sections occur in everyday life.		
<ul> <li>Students will understand that:</li> <li>Equations of conic sections can be reorganized and analyzed to produce adequate graphs</li> <li>Common shapes known in Geometry have complex Algebraic equations.</li> <li>Conic sections, parametric equations and the polar coordinate system are the basis of higher level Physics applications</li> </ul>	<ul> <li>Essential Questions:</li> <li>What is the importance of conic sections?</li> <li>Is a graph that overlaps itself possible, if it only has one equation?</li> </ul>	
Students will know: • Standard form of a circle • Standard form of a parabola • Standard form of an ellipse • Standard form of a hyperbola	<ul> <li>Students will be able to:</li> <li>Identify Conics from graph OR equation in any form</li> <li>Write standard equations of conics</li> <li>Graph conics</li> </ul>	
Stage 2: Acceptable Evidence		

## Transfer Task

Conics Section Project- This is a two-part project. In the first part of the project, students will be asked to investigate where conic sections occur in real-life. In the second part of the project, students will be asked to re-create how each of the conic sections are formed.

- Trigonometry with Calc Chat and Calc View (10 E) ٠
- TI-Nspire Lesson Activities: https://education.ti.com/en/timathnspired/us/precalculus •
- Folding Conic Sections Activity •
- Conics Formula Sheet •
- Conics Quiz Review •
  - Conics Review Answers
- Khan Academy Conics ٠
- Summative Assessment Tasks ٠